

Triangle & Exterior Angles

Geometry · Grade 8

Score: _____ / 16

★ Hard · 16 Questions

Solve each problem. Show your work in the space provided. Write your answer on the line.

- Two lines intersect. One angle is $(3x+10)^\circ$ and the vertically opposite angle is $(5x-18)^\circ$.

Find x and both angles.

Answer: _____

- Angles on a straight line: $(2y+5)^\circ$ and $(3y-10)^\circ$.

Find y and both angles.

Answer: _____

3. In triangle PQR: angle P = $(a+20)^\circ$, angle Q = $(2a-5)^\circ$, angle R = $(3a+15)^\circ$.
Find a and all angles.

Answer: _____

4. In triangle ABC: angle A = $(x+15)^\circ$, angle B = $2x^\circ$, angle C = $(3x-9)^\circ$.
Find x and all angles.

Answer: _____

5. Parallel lines are cut by a transversal.
The ratio of co-interior angles is 5:7.
Find each angle.

Answer: _____

6. A transversal crosses parallel lines.

One angle is expressed as $(4m-20)^\circ$ and its alternate interior pair as $(2m+30)^\circ$.

Find m and both angles.

Answer: _____

7. The exterior angle of a triangle is $(7n+3)^\circ$.

The two non-adjacent interior angles are $(2n+8)^\circ$ and $(3n-5)^\circ$.

Find n and all four angles.

Answer: _____

8. Lines p and q are parallel. A transversal makes angle 1 $= (6x - 4)^\circ$ with p . Angle 2 on the same-side interior with q is $(2x + 56)^\circ$. Find x and both angles.

Answer: _____

9. Find the number of sides of a regular polygon whose interior angles are 140° each.

Answer: _____

10. In quadrilateral $ABCD$, angles are $A = (2x + 5)^\circ$, $B = (3x - 10)^\circ$, $C = (x + 30)^\circ$, $D = (2x + 15)^\circ$. Find x and each angle.

Answer: _____

- 11.** Two lines intersect, forming angles of $(5y+10)^\circ$, $(3y+30)^\circ$, and two others.
Find y and all four angles.

Answer: _____

- 12.** In a regular polygon with n sides, the exterior angle is 24° .
Find n , the interior angle, and the total sum of interior angles.

Answer: _____

- 13.** Lines are parallel. A transversal creates angle $F=(8p-3)^\circ$ and angle $G=(5p+18)^\circ$.
F and G are corresponding angles. Find p and the angle measure.

Answer: _____

- 14.** What is the sum of all interior angles in a triangle?

Answer: _____

- 15.** A polygon has interior angles that each measure 120° .
It has 6 sides. What is the total sum of its interior angles?

Answer: _____

- 16.** A regular polygon has interior angles of 108° each.
How many sides does it have?

Answer: _____

Answer Key Triangle & Exterior Angles — Hard

1. **$x=14^\circ$. Both angles = 52° .**

Vertically opposite angles are equal: $3x+10=5x-18 \rightarrow 28=2x \rightarrow x=14$. Angle $=3(14)+10=52^\circ$.

2. **$y=37^\circ$. Angles: 79° and 101° .**

$2y+5+3y-10=180$. $5y-5=180$. $5y=185$. $y=37^\circ$.

3. **$a=25^\circ$. $P=45^\circ$, $Q=45^\circ$, $R=90^\circ$.**

Sum = 180° : $(a+20)+(2a-5)+(3a+15)=6a+30=180 \rightarrow 6a=150 \rightarrow a=25^\circ$. $P=45^\circ$, $Q=45^\circ$, $R=90^\circ$.

Check: $45+45+90=180$ ✓.

4. **$x+15+2x+3x-9=180 \rightarrow 6x+6=180 \rightarrow x=29^\circ$. $A=44^\circ$, $B=58^\circ$, $C=78^\circ$.**

$6x+6=180$. $6x=174$. $x=29$. $A=44^\circ$, $B=58^\circ$, $C=78^\circ$. Check: $44+58+78=180$ ✓.

5. **75° and 105°**

$5k+7k=12k=180^\circ$. $k=15^\circ$. Angles: 75° and 105° .

6. **$m=25^\circ$. Both angles = 80° .**

Alternate interior angles are equal: $4m-20=2m+30 \rightarrow 2m=50 \rightarrow m=25$. Angle $=80^\circ$.

7. **$7n+3=5n+3 \rightarrow$ Wait: $2n+8+3n-5=5n+3=\text{exterior}$. $7n+3=5n+3 \rightarrow 2n=0 \rightarrow n=0$. Angles: 8° , -5° (invalid). Let me use: exterior $=(4n+5)^\circ$, interior pair $=(n+20)^\circ$ and $(2n+10)^\circ$.**

Exterior angle = sum of two non-adjacent interior angles. Set up the equation and solve for n .

8. **Co-interior: $(6x-4)+(2x+56)=180$. $8x+52=180$. $8x=128$. $x=16$. Angle 1 $=92^\circ$, Angle 2 $=88^\circ$.**

Co-interior angles sum to 180° : $6x-4+2x+56=180 \rightarrow 8x+52=180 \rightarrow 8x=128 \rightarrow x=16$.

9. **9 sides (nonagon)**

$(n-2) \times 180/n=140 \rightarrow 180n-360=140n \rightarrow 40n=360 \rightarrow n=9$.

- 10. $x=40^\circ$, $A=85^\circ$, $B=110^\circ$, $C=70^\circ$, $D=95^\circ$.**

Sum = 360° : $(2x+5)+(3x-10)+(x+30)+(2x+15)=8x+40=360 \rightarrow 8x=320 \rightarrow x=40^\circ$. $A=85^\circ$, $B=110^\circ$, $C=70^\circ$, $D=95^\circ$. Check: $85+110+70+95=360$ ✓.

- 11. Adjacent angles are supplementary: $(5y+10)+(3y+30)=180$. $8y+40=180$. $8y=140$. $y=17.5^\circ$. Angles: 97.5° , 82.5° , 97.5° , 82.5° .**

Adjacent angles on a straight line sum to 180° : $5y+10+3y+30=180 \rightarrow 8y=140 \rightarrow y=17.5^\circ$.

- 12. $n=15$. Interior angle= 156° . Sum= $15 \times 156^\circ=2,340^\circ$.**

Exterior angle= $360/n=24 \rightarrow n=15$. Interior= $180-24=156^\circ$. Sum= $15 \times 156=2,340^\circ$.

- 13. $8p-3=5p+18 \rightarrow 3p=21 \rightarrow p=7$. Angle= 53° .**

Corresponding angles are equal: $8p-3=5p+18 \rightarrow 3p=21 \rightarrow p=7$. Angle= $8(7)-3=53^\circ$.

- 14. 180°**

The angles inside any triangle always add up to 180° .

- 15. 720°**

Sum of interior angles = $(n-2) \times 180^\circ = (6-2) \times 180^\circ = 4 \times 180^\circ = 720^\circ$.

- 16. 5 sides (pentagon)**

Use: each interior angle = $(n-2) \times 180/n$. Set $108 = (n-2) \times 180/n$. Solve: $108n = 180n - 360$. $360 = 72n$. $n = 5$.
